## THE CONCEPTS OF *DEŚĀNTARA* AND *YOJANA* IN INDIAN ASTRONOMY

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**Abstract:** In this paper we discuss in detail the concepts of (i) the *deśāntara* correction to the mean longitude of a heavenly body, and (ii) the linear distance, called *yojana*. We consider the definitions and procedures given in classical Indian astronomical texts like the *Ārybhaṭīyam*, *Brāhmasphuṭasiddhānta*, *Khaṇḍakhādyaka*, *Laghu- Mahā-Bhāskarīya*, *Siddhānta Śiromaṇi*, *Grahalāghavam* and *Tantrasaṅgraha*. From our findings we notice that there were apparently two distinct schools (*paksas*), which were led by Ārybhaṭa (b. CE 476) and Brahmagupta (ca. 628), who used 1050 and 1581 *yojana*, respectively, for the diameter of the Earth.

Keywords: Indian astronomy, deśāntara, yojana

#### 1 INTRODUCTION

Since the Earth rotates about its own axis from west to east sunrise takes place earlier for places with eastern longitudes and later for those with westernlongitudes. In classical Indian astronomical texts, the time during a day was reckoned from the instant of local sunrise. But the procedures for the computation of the mean positions of the heavenly bodies were given in the texts with reference to the mean sunrise for the prime meridian of Ujjayinī (in present-day Madhya Pradesh). The meridian through Ujjayinī was assumed to pass through a few more important places, like Kurukṣetra, and intersect the terrestrial equator at Laṅkā.

Therefore while computing the mean positions of the heavenly bodies for a given local time at a given place a correction, called the deśāntara saṃskāra, had to be applied to account for the longitudinal difference between that place and Ujjayinī. The computation of the deśāntara correction needed the longitudinal difference between the given place and the prime meridian through Ujjayinī. In the classical texts this distance was expressed in terms of the linear difference between the two places. For this purpose, the Earth's circumference in yojanas was required. At that time, there were two main schools (pakṣas), and they took the

Earth's circumference to be about 3300 *yojanas* and 4800 *yojanas* respectively

## 2 THE *DEŚĀNTARA* ACCORDING TO DIFFERENT TEXTS

In Indian astronomy linear distances were measured in *yojanas*. In Figure 1 *PQAC* is the prime meridian through Ujjayinī. *PDBQ* is the meridian

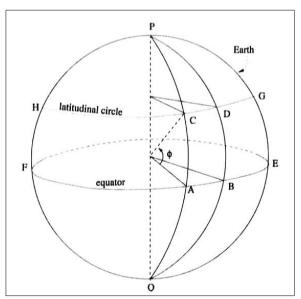


Figure 1: The longitude and latitude lines of a given place (diagram: Padmaja Venugopal).

and through the observer. *ABEF* is the terrestrial equator with circumference given as 3300 *yojanas* in the Ārya *pakṣa. CDGH* is a latitudinal circle corresponding to the latitude  $\phi$ . The radius of this circle (a small circle) is the radius of the sphere (R) multiplied by  $cos\phi$ . The circumference of this latitudinal circle ( $C_0$ ) is given by

$$C_0 = (3300 \times R\cos\phi)/R = 3300\cos\phi.$$
 (1)

The time taken by the Earth to complete one revolution (360°) is 60 *ghaţīs*, and this corresponds to one full rotation of the latitudinal circle  $C_0$ .

According to the *Tantrasangraha* of Nīlakantha Somayājī (Ramasubramanian and Sriram, 2011) the equatorial circumference is about 3300 *yojanas*, and so the equatorial radius is  $3300/2\pi = 525.211 \approx 525$  *yojanas*. The Earth's known radius is approximately 4000 miles. Therefore, 525 *yojanas*  $\approx$  4000 miles, and 1 *yojana* =  $160/21 = 7.619 \approx 7.6$  miles.

Table 1: Deśāntara corrections for heavenly bodies (after Sastri, 2006).

Heavenly Bodies	Mean Daily Motion	Deśāntara Correction
Ravi	00 59 08	00 28
Candra	13 10 35	06 25
Kuja	00 59 08	00 15
Budha	04 05 32	01 59
Guru	00 04 59	00 02
Śukra	01 36 08	00 47
Śani	00 02 00	00 01
Candrocca	00 06 41	00 03
Rāhu	00 03 11	00 03

### 2.1 The Deśāntara According to the Ganakānanda

The *Gaṇakānanda was* authored by Sūryācārya, the son of Bālāditya, who came from the Andhra region. The text was based on the *Sūryāsiddhānta*, and it belongs to the *Saurapaksa*. The epochal date of the text is CE 16 March 1447. The currently available text is a single Sanskrit text in the Telugu script, edited and published by Chella Lakshmi Narasimha Sastri from Machalipatnam in the Andhra region and reprinted in the year 2006:

lakāvantīpurīmadhyarekhāpūrvāparast hitai l yojanairgatayonighnaḥkhakhāṣṭanigam

ai r hṛtāh II (Sastri, 2006).

The *deśāntara* is obtained in arc seconds by multiplying the *yojanas* of a given place from the north-south line ( $rekh\bar{a}$ ) passing through Laṅkā and Avantī Ujjayinī by the mean daily motion and dividing by 4800. Taking the Earth's circumference as 4800 *yojanas* we get the Earth's radius as 4800/ $\pi$  = 763.94. Assuming the Earth's radius as 800 *yojanas*, its circumference is  $2\pi \times 800 = 4800$  *yojanas*. According to Sastri (2006),

the *yojanas* of Machilipatanam is 39. So the *deśāntara* correction for *Ravi* is (59' 08"/4800) × 39 = 0' 28". Similarly, *deśāntara* corrections for other bodies were computed, and are listed in Table 1.

In his commentary, Yallaya, the well-known fifteenth century Andhra astronomer, gives the distance of Skandaśomesvara from the Ujjayinī meridian as 36 *yojanas* according to the *Sūryā-siddhānta* (Gangooly, 1989; Parameśvara, 1957). But according to Ārybhaṭa (Sambasivasastri, 1977; Shukla and Sarma, 1976) it is 23<sup>7</sup>/15 *yojanas*. In our modern reckoning, Skandaśomesvara has a longitude of 79° 50′ E and a latitude of 15° 30′ N. The longitudinal distance of this place is 04° 05′ to the east of Ujjayinī (which has a longitude of 75° 45′ E). Therefore,

$$R = (360^{\circ} \times 36)/[2\pi \cos\phi(L - 75^{\circ} 45')] \approx 524$$
 yojanas, (2)

and according to Yallaya the Earth's circumference is 3292 ≈ 3300 *yojanas* (Gangooly, 1989; Parameśvara, 1957).

## 2.2 The Earth's Diameter and Circumference According to the *Khaṇḍakhādyaka*

The Khaṇḍakhādyaka of Brahmagupta (CE 665) follows Ārybhaṭa's Ārdharātrika system (see Chatterjee, 1970; Sengupta, 1934). In the Gītika pāda of the Āryabhaṭīyam the description of the deśāntara correction is given in Śloka 7, which is quoted below:

nṛ- ṣi yojanaṃ ñilā bhūvyāso' rkendvorghrñā giṇa ka meroḥ| (Shukla and Sarma, 1976, Chapter 1: śl. 7).

According to the  $\bar{A}ryabhat\bar{\imath}yam$  (Sambasivasastri, 1977; Shukla and Sarma, 1976: Chapter 4,  $\pm$  sl. 39, 40) the Earth's diameter is 1050  $\pm$   $\pm$  yojanas. Therefore, the circumference is 1050  $\pm$   $\pm$  3298.6722  $\pm$  3300  $\pm$  3956.55 miles), and 1  $\pm$  3956.55 miles), and 1  $\pm$  3956.55 miles. Note (i) If we take the circumference as 3200  $\pm$  3200 yojanas, then the radius is 509.2958  $\pm$  3200 yojanas = 7.76866 miles; and (ii) Sometimes for the purposes of easy calculation, the Earth's circumference is taken as 3200 yojanas.

## 2.3 The Deśāntara According to the Grahalāghavam

Ganesa Daivajña (CE 1520) in his *Grahalā-ghavam* refers to the *desāntara* in Chapter 1 as:

nijanijapurarekhāntastitadyojanaughād rasalavamitaliptāḥ:

svarṇamindupareprāk II (Rao and Uma, 2006: madhyamādhikara, śl. 9).

To find the *deśāntara* correction for the Moon, the distance of the given place from the Ujjayinī meridian in *yojanas* is divided by 6 to

get it in *liptās* (*kalās*). Gaņeśa takes, for easy calculation the Moon's daily motion as 800' and the Earth's circumference as 4800 *yojanas* (see Pandey, 1994; Rao, and Uma, 2006). Therefore the *deśāntara* correction is (*yojanas* × daily motion)/4800 = *yojanas*/6 *kalās*. We know that the equatorial radius and polar radius are respectively 3963.2 and 3949.91 miles. The average of the two values is 3956.55 miles. Bhāskara II's value for the circumference of the Earth is 4967 *yojanas* (Mishra, 1991). Therefore, the radius is 790.5 *yojanas* = 3956.55 miles. Therefore, 1 *yojana* = 5.00512334 miles  $\approx$  5 miles. Along the small circle through *Kāśī* the arc length is 90° 37′ 50″.

Note that (i) in his Hindi commentary on the *Grahalāghavam* Joshi (1981: 30) takes the distance of *Kāśī* as 64 *yojanas* quoting the *prācīna āchāryas*); and (ii) Pandey (1994: 17) takes 1 *yojana* as 8 miles. This is not correct. According to the *Grahalāghavam*, it works out at about 5 miles.

According to the *Tantrasangraha* (Ramasubramanian and Sriram, 2011) the equatorial circumference is 3300 *yojanas* and hence the equatorial radius is  $3300/2\pi = 525.211 \approx 525$  *yojanas*. Since the Earth's known radius is approximately 4000 miles, 525 *yojanas* = 4000 miles. Therefore, 1 *yojana* is  $160/21 = 7.619 \approx 7.7$  miles.

According to the *Vaṭeśvara Siddhānta* & *Gola* (Shukla, 1985–1986: 135) the Earth's equatorial diameter is 1527 *yojanas*. The Earth's circumference is  $(1054 \times 3927)/1250 = 3311.2464$  *yojanas*  $\approx 3311$  *yojanas*.

In his *Khaṇḍakhādyaka* Brahmagupta gives the Earth's circumference as 4800 *yojanas* (Chatterjee, 1970(1): 50). But in the *Uttara Khaṇḍa-khādyaka* he gives the correct method to obtain the circumference of a small circle through the place. Here he gives the circumference of the small circle as  $5000 \cos \phi$  *yojanas*. Therefore, the Earth's radius is  $5000/2\pi = 795.77$  *yojanas* =  $5000/2\sqrt{10} = 790.569$  *yojanas*.

## 2.4 The Karanakutūhalam of Bhaskara II

In his *Karaṇakutūhalam* Bhaskara II considers the circumference of the Earth as 4800 *yojanas* (Mishra, 1991). To cover 4800 *yojanas* the Earth takes 60 *ghatīs*. For 1 *yojana* the time taken is therefore 60/4800 = 1/80 *ghatīs*. Therefore in his translation of the *Sūryasiddhānta*, Burgess gives the Earth's circumference for the circumference of a small circle through Washington ( $\phi = 38^{\circ} 54'$ ) as  $2\pi rcos\phi = 5059.556 \times cos(38^{\circ} 54') = 3937.56$  *yojanas* (Gangooly, 1989: 43–45, *śl.* 60–61). The *Karaṇakutūhalam* defines the *de-śāntara* correction (Mishra, 1991: Chapter 1, *śl.* 15) as (yojanas/90) × daily motion.

Values for the circumference of the Earth in *yojanas* vary according to the sources consulted. For example, in his *Siddhānta Śiromani* Bhaskara II gives the Earth's circumference as 4967 *yojanas* and its diameter as 1581 *yojanas*:

proktoyojanasankhyayākuparidhiḥsaptā nganandābḍhayas tadvyasaḥkubhujangasāyakabhuvothap rocyateyojanam I yamyodakpurayohpalāntarahatambhuv eṣṭanaṃbhāmśa h t tadbhaktasyapurantarādhvanaiha j ñeyaṃsamamyojanam II (Arkasomayaji, 1980; Vāsanā, 1929: bhuparidhi, 1).

## 2.5 The Deśāntara According to the Vākya Karaṇa

According to the *Vākya Pañcādhyāyi* (Kuppanna Sastry and Sarma, 1962: 255, *śl.* 16)

deśāntarād yojanāḥ syurnāḍya maṇihṛtaṃ phalam | tādhanaṃ samarekhāyāḥ pañcaccedanyathā kṣayaḥ

the Earth's circumference is 3300 yojanas, which converting to nādyas is 60/3300 = 1/55. The Pañcāsiddhāntikā gives the deśāntara of Pudukottai (latitude: 10° 23' N; longitude: 78° 52' E) as an example (Sarma, 1993). It is 24.4 (E) yojanas from Ujjayini. Then

 $[(L_1 - L_u)/360] \times c = [(78^{\circ} 52' - 75^{\circ} 45')/360] \times c$ = 24.4  $\Rightarrow$  c = 2818.396 yojanas. Now suppose that  $2\pi r \cos \phi = 2818.396$  yojanas. Then  $2\pi r \cos (10.4^{\circ}) = 2818.396/(2\pi \times 0.98357)$  and r = 456.0546326.

The late Professor Kuppanna Sastry comments on the *Āryapaksa* and *Saurapaksa* in respect of the Earth's equatorial circumference as follows:

But it is to be noted that in the Ardharātrika of Āryabhaṭa and in the Khanda Khadyaka, the diameters of the earth is given as 1600 yojanas from which the equatorial circumference got is 5027 yojanas. Therefore the original Saura must have given the same values. The modern Sūrya siddhānta and the siddhantas that follow it also give the same. From this the latitude circle at or near Ujjaini should be given according to them as 5027cos24° = 4600 yojanas. According to the Āryabhaṭīya which uses a yojana measure one and a half times that of Saura etc., the equatorial circumference would be 3300 yojanas. From this, it is 14° latitude circle that would be 3200 yojanas and not the Ujjaini latitude circle. (see Sarma, 1993: 210).

## 2.6 The Deśāntara According to the Pauliśa Siddhāntha

Yavanantarajya nādyaḥ sapṭā'vantyāṃ tribhāgasaṃyuktāḥ | Vārāṇasyam trikṛtiḥ' sādhanamanyatra vaksyāmi || (śl.13).

The time correction for the longitude of Yavanapura (Alexandria) relative to Ujjayinī is 7  $n\bar{a}$  $\dot{q}$ ikās (na) 20  $vin\bar{a}$  $\dot{q}$ ikās (vin) and to Vārāṇasī is 9  $n\bar{a}$  $\dot{q}$ ikās. Note that according to Kuppanna Sastry (Sarma, 1993) these are respectively (75° 50′ - 30°)/6 = 7na 38vin and (83° - 30°)/6 = 8na 50vin. Therefore the distance between Yavanapura and Ujjayinī is [(7 - 20)/60]  $\times$  3300 yojanas = 403120 yojanas, and between Yavanapura and Vārāṇasī is (9  $\times$  3300)/60 = 495 yojanas.

For Pudukottai (longitude 78° 52′ E and latitude 10° 23′ N),  $(L - L_0)/360 = 24.4/ccos\phi$  (i.e.  $\phi = 10^\circ 23'$  N);  $(L - L_0)/360 = 24.80633/c$ , or  $c = 24.80633/(L - L0) \times 360 = 2865.6$ .

Note that the modern value for Earth's circumference is  $2\pi \times 4000 = 8000 \pi$  miles. In the Saurasiddhānta (Sarma, 1993: 209, śl. 10) 1 nādī =  $53\frac{1}{3}$  yojanas. Therefore, 60 nādīs =  $60 \times 53.333 \approx 3200$  yojanas. Taking the circumference as 3200 yojanas, we have 60 nādīs = 3200 yojanas. Therefore, 1 nādī =  $3200/60 = 160/3 = 53\frac{1}{3}$  yojanas.

According to the *Pañcasiddhānta* (Sarma, 1993: 52), the longitudes of Kurukshetra and Ujjayinī are 76° 51′ and 75° 45′ respectively. Then (1° 06′/360) × 3300 = 10.8 *yojanas*, and (1° 06′/360) × 4800 = 14.66 *yojanas* ≈ 15 *yojanas*. The number of *yojanas* along the latitude circle is given by  $15\cos\phi = 12.9947 \approx 13$  *yojanas*.

## 2.7 The Concept of the *Deśāntara* and *Yojana* in Indian Astronomy

The Earth's circumference is  $360^{\circ}$  which equals  $4800 \ yojanas$ . The longitude of Bangalore is  $1^{\circ}$  50' east of Ujjayinī). For  $1^{\circ}$  50' we have  $(1^{\circ}$  50')/360 ×  $4800 = 24.26 \ yojanas$ .

For Machalipattanam,  $[(L-L_0)/360] \times 4800$  yojanas =  $(5.366/360) \times 4800$  yojanas. Note that along the small circle through Machalipatnam the circumference  $\approx 4606.799041$  yojanas. Therefore, the distance from Machalipatnam to the Ujjayinī meridian is 69.04677. The circumference of the small circle through a specific place is given by  $(2\pi R)\cos\phi$ , where R is the Earth's radius =  $4800\cos\phi$  yojanas.

For Bangalore (present-day Bengaluru),  $4800\cos 13^\circ = 4676.976$  yojanas. Then, (1° 5′/ 360) × 4676.976 yojanas = 23.8179 yojanas. Taking the Earth's circumference as 3200 yojanas,  $23.8179 \times (3200/4800) = 15.8786$  yojanas.

For Machalipattinam, the circumference of a small circle is  $4800\cos(16^{\circ}\ 11') = 4609.799$  *yojanas*. If we take circumference as 39 *yojanas*,  $(360^{\circ}\times 39)/5.3667 = 2626$  *yojanas*. Therefore, the equatorial circumference is  $2616/\cos 16^{\circ}\ 11' = 2749$  *yojanas*.

# 2.8 The *Deśāntara A*ccording to Modern Astronomy:

The longitudes of Kāśī and of Ujjayinī are 83° 01' and 75° 45' respectively. The difference in longitudes is 7° 16', therefore (7° 16'/360°)  $\times$  4967 = 100115135 *yojanas* along the equator. The equatorial diameter is 12756 km, the circumference is 40090 km, and the radius is 6378/1.6 km = 3986.25 miles.

#### 3 CONCLUDING REMARKS

A fairly elaborate analysis of the concept of the deśāntara—resulting in the time of local sunrise due to the Earth's rotation—has been presented in this paper. We have discussed the effect of the difference in longitudes of a given place and the then-adopted central meridian (of Ujjayinī) on the local time.

The linear distance between the places was measured in terms of a unit of distance called a vojana. This unit is defined in terms of the circumference and the diameter of the Earth. We examined important texts like the *Āryabhatiyam*, Pañcasiddhāntā, Sūryasiddhānta, Khandakhādvaka, Siddhanta Śiromni, Grahalāghavam, Karanakutūhalam, Tantrasangraha and the Vākya Karana, and we found that the main pakṣas (Schools) adopted different values for the circumference (paridhi) of the Earth. The Aryapakṣa adopted a value of 3300 yojanas, the Brāmhapakṣa 4967 yojanas and the Saurapakṣa 4800 yojanas. These values were compared using the modern known values for the equatorial circumference and diameter of the Earth.

The three *pakṣas* were founded at about the same time (around the sixth century CE), but tended to flourish in different parts of India: the *Āryapakṣa* in Southern India, the *Brāmhapakṣa* in western and north-western India, and the *Saurapakṣa* in northern and eastern India. The fact that the two more northerly *pakṣas* have rather similar values for the circumference of the Earth and that they differ markedly from the value used by the southern *pakṣa* is interesting, but the precise reasons why the adopted values were so different is not known. Plofker (2009: 70) writes:

The sources of competing parameters and authors' reasons for choosing them are not always clear ... a frequently stated motive is the desire to harmonize astronomical calculations as far as possible with *smṛti* trad-

itions about cosmological time, or to bring them into agreement with observed positions.

Yet these reasons can hardly apply in the case of the circumference of the Earth, so further research is required in order to explain these differences.

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#### **5 BIBLIOGRAPHY**

- Arkasomayaji, D. (transl.), 1980. Siddhānta Śiromani of Bhāskaracharya. Tirupati, Kendriya Sanskrit Vidyapeetha.
- Chatterjee, B. (ed. and transl.), 1970. The Khandakhādyaka (an Astronomical Treatise) of Brahmagupta: with the commentary of Bhattotpala. Two Volumes. New Delhi, Motilal Banarsidass.
- Gangooly, P. (ed.), 1989. The Sūryasiddhānta, translated by the Reverend E. Burgess ... and Introduction by P.C. Sengupta. Delhi, Motilal Banarsidass.
- Joshi, K. (comm.), 1981. The Grahalāghavam of Gaņeśa Daivajña, with a commentary by Mallāri and Viśvanātha ... Varanasi, Motilal Banarsidass.
- Kuppanna Sastry, T.S., and Sarma, K.V. (eds.), 1962.
  Vākya Pañcādhyāyi. Madras. K.S. Research Institute.
- Kuppanna Sastry, T.S (transl. and notes), 1993. *Pañ-casiddhāntikā of Varāhamihira*. Madras, P.P.S.T. Foundation.
- Mishra, A.R. (comm.), 1982. *The Makarandasārinī* ... Varanasi, Madālasā Publications.
- Mishra, S. (transl.), 1991. The Kāranakutūhalam of Bhāskara II, with a commentary by Sumatiharsa and Sudhākara Dvivedi ... Varanasi, Oriental Publishers (Krishnadas Academy).
- Pandey, R.C. (ed.), 1994. The Grahalāghavam of Gaņeśa Daivajña, with a Hindi commentary by Mallāri ... Varanasi, Chowkhamba Sanskrit Series.
- Parameśvara (ed.), 1957. *The Sūryasiddhānta ...* Lucknow, K.S. Shukla.
- Plofker, K., 2009. *Mathematics in India*. Princeton, Princeton University Press.
- Ramasubramanian, K., and Sriram, M.S., 2011. *The Tantrasaṅgraha of Nīlakaṇṭha Somayājī.* New Delhi, Hindistan Book Agency.
- Rao, S. Balachanra, 2000. *Ancient Indian Astronomy Planetary Positions and Eclipses*. Delhi, B.R. Publishing.
- Rao, S. Balachandra, 2000. *Indian Astronomy An Introduction*. Hyderabad, Universities Press.
- Rao, S.B., and Uma, S.K. (trans.), 2006. *The Grahalāghavam of Gaņeśa Daivajña ...* New Delhi, Indian National Science Academy.
- Rao, S. Balachandra, 2008. *Indian Astronomy A Primer*. Bengalaru, Bhavan's Gandhi Centre of Science and Human Values.
- Rao, S. Balachandra, and Venugopal, P., 2008. *Eclipses in Indian Astronomy*. Bangalore, Bhavan's Gandhi Centre of Science and Human Values.
- Rao, S. Balachandra, and Venugopal, P., 2009. Transits and Occultations in Indian Astronomy. Bangalore, Bhavan's Gandhi Centre of Science and

- Human Values.
- Rao, S. Balachandra, 2016. Indian Astronomy Concepts and Procedures. Bengaluru, M.P. Birla Institute of Management.
- Rupa, K., Venugopal, P., and Rao, S. Balachandra, 2014. Makarandasārinī and allied Saurapaksa tables —a study. *Indian Journal of History of Science*, 49, 186–208.
- Sambasivasastri, K. (ed.), 1977. The Āryabhaṭīyam of Āryabhaṭa, with a commentary by Nīlakaṇṭha Somasutvan ... Trivandrum, K. Sambasivasastri (reprint).
- Sarma, K.V. (trans.), 1993. The Pañcasiddhāntikā of Varāhamihira, English translation and notes by T.S. Kuppana Sastry ... Madras, P.P.S.T. Foundation.
- Sastri, C.L.N. (ed.), 2006. *The Gaṇakānanda, Sans-krit text in Telugu script ...* Machalipatnam, Chella Lakshmi Narasimha Sastri (reprint).
- Sengupta, P.C. (ed. and transl.), 1934. *The Khaṇḍa-khādyaka of Brahmagupta*. Calcutta, University of Calcutta.
- Shukla, K.S. (ed. and transl.), 1985–1986. The Vaţeśvara Siddhānta & Gola. New Delhi, INSA.
- Shukla, K.S., and Sarma, K.V. (eds.), 1976. The Āryabhatīyam of Āryabhaṭa. New Delhi, Indian National Science Academy.
- Tandan, V. (comm.), 1945. *The Makarandasārinī* ... Bombay, Sri Venkateshwara Press.
- Vāsanā (ed.), 1929. The Siddhānta Śiromani of Bhāskara II, with Bhāskara's commentary ... Benaras, Sudhakara Dvivedi (Kashi Skt. Series, No.72).



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Professor S. Balachandra Rao has an MSc (Mathematics) from the University of Mysore and a PhD (Fluid Mechanics) from Bangalore University. He served at the National Colleges at Gauribidanur and Bangalore, teaching mathematics for 35 years, and retired in 2002 as Principal. Currently he is (1) Honorary Director, Gandhi Centre of Science

and Human Values, Bharatiya Vidya Bhavan, Bengaluru; (2) a Member of the National Commission for History of Science, INSA, New Delhi; and (3) an Honorary Senior Fellow at the National Institute of Advanced Studies (NIAS) in Bengaluru. Professor Rao has been researching in the field of classical Indian astronomy since 1993 under successive research projects from INSA. He has authored, singly and jointly, quite a few papers in reputed journals and books on Indian mathematics and astronomy. The books published so far are about 30, half in English and the remainder in Kannada. The more popular ones among them are: (1) Indian Mathematics and Astronomy—Some Landmarks; (2) Indian Astronomy—Concepts and Procedures; (3) Eclipses in Indian Astronomy; (4) Transits and Occultations in Indian Astronomy [titles (3) and (4) were co-authored by Dr Padmaja Venugopal]; (5) Grahalaghavam of Ganesha Daivaina, English Translation and Notes; (6) Karanakutuhalam of Bhaskara II, English Translation and Notes [titles (5) and (6) were co-authored by Dr S.K. Uma]; (7) Astrology-Believe it or Not?; (8) Traditions, Science and Society, etc. While title (7) was translated into the Kannada and Marathi languages, title (8) was rendered into Kannada, Telugu and Malavalam versions. The Kannada versions of books (7) and (8) have won awards as "The Best Works of Rational Literature" from the Kannada Sahitya Parishat (Kannada Literary Authority).